

2. The number of defects per metre in a roll of cloth has a Poisson distribution with mean 0.25

Find the probability that

(a) a randomly chosen metre of cloth has 1 defect, (2)

(b) the total number of defects in a randomly chosen 6 metre length of cloth is more than 2 (3)

A tailor buys 300 metres of cloth.

(c) Using a suitable approximation find the probability that the tailor’s cloth will contain less than 90 defects. (5)

Lined area for student response



3. An online shop sells a computer game at an average rate of 1 per day.
- (a) Find the probability that the shop sells more than 10 games in a 7 day period. (3)

Once every 7 days the shop has games delivered before it opens.

- (b) Find the least number of games the shop should have in stock immediately after a delivery so that the probability of running out of the game before the next delivery is less than 0.05 (3)

In an attempt to increase sales of the computer game, the price is reduced for six months. A random sample of 28 days is taken from these six months. In the sample of 28 days, 36 computer games are sold.

- (c) Using a suitable approximation and a 5% level of significance, test whether or not the average rate of sales per day has increased during these six months. State your hypotheses clearly. (7)



4. A continuous random variable X is uniformly distributed over the interval $[b, 4b]$ where b is a constant.

(a) Write down $E(X)$.

(1)

(b) Use integration to show that $\text{Var}(X) = \frac{3b^2}{4}$.

(3)

(c) Find $\text{Var}(3 - 2X)$.

(2)

Given that $b = 1$ find

(d) the cumulative distribution function of X , $F(x)$, for all values of x ,

(2)

(e) the median of X .

(1)



5. The continuous random variable X has a cumulative distribution function

$$F(x) = \begin{cases} 0 & x < 1 \\ \frac{x^3}{10} + \frac{3x^2}{10} + ax + b & 1 \leq x \leq 2 \\ 1 & x > 2 \end{cases}$$

where a and b are constants.

(a) Find the value of a and the value of b . (4)

(b) Show that $f(x) = \frac{3}{10} (x^2 + 2x - 2)$, $1 \leq x \leq 2$ (1)

(c) Use integration to find $E(X)$. (4)

(d) Show that the lower quartile of X lies between 1.425 and 1.435 (3)



Question 5 continued

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Q5

(Total 12 marks)



- 6. In a manufacturing process 25% of articles are thought to be defective. Articles are produced in batches of 20
 - (a) A batch is selected at random. Using a 5% significance level, find the critical region for a two tailed test that the probability of an article chosen at random being defective is 0.25
You should state the probability in each tail which should be as close as possible to 0.025
- (5)**

The manufacturer changes the production process to try to reduce the number of defective articles. She then chooses a batch at random and discovers there are 3 defective articles.

- (b) Test at the 5% level of significance whether or not there is evidence that the changes to the process have reduced the percentage of defective articles. State your hypotheses clearly.
- (5)**



7. A telesales operator is selling a magazine. Each day he chooses a number of people to telephone. The probability that each person he telephones buys the magazine is 0.1

(a) Suggest a suitable distribution to model the number of people who buy the magazine from the telesales operator each day. (1)

(b) On Monday, the telesales operator telephones 10 people. Find the probability that he sells at least 4 magazines. (3)

(c) Calculate the least number of people he needs to telephone on Tuesday, so that the probability of selling at least 1 magazine, on that day, is greater than 0.95 (3)

A call centre also sells the magazine. The probability that a telephone call made by the call centre sells a magazine is 0.05

The call centre telephones 100 people every hour.

(d) Using a suitable approximation, find the probability that more than 10 people telephoned by the call centre buy a magazine in a randomly chosen hour. (3)



